











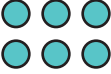





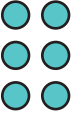

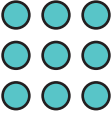

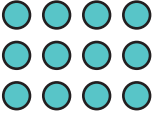





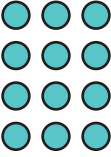

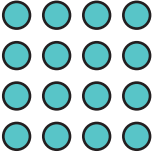




# Recognizing Rectangular Arrays

NCTM Standards 1, 2, 6, 8, 10

How many dots?

<p>1</p>  	<p>2</p>  	<p>3</p>  	<p>4</p>  
<p>5</p>  	<p>6</p>  	<p>7</p>  	<p>8</p>  
<p>9</p>  	<p>10</p>  	<p>11</p>  	<p>12</p>  
<p>13</p>  	<p>14</p>  	<p>15</p>  	<p>16</p>  

 **17** Sometimes the same array is shown in two problems above. List the pairs of problems that have the same array and explain why the pairs match.

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- 18 In the third grade classroom, there are 4 rows of chairs. Each row has 3 chairs. How many chairs are in the classroom? Draw a picture to show how you solve the problem. Write a number sentence to show your answer.

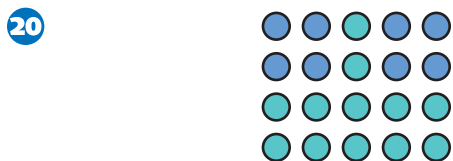
chairs in the classroom

### How many dots?



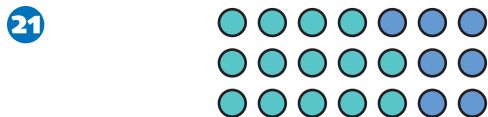
$$\square + \square = \square$$

total



$$\square + \square = \square$$

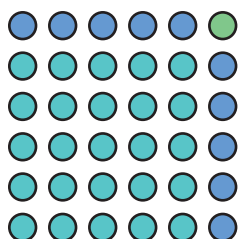
total



$$\square + \square = \square$$

total

### 22 Challenge



$$\square + \square + \square = \square$$

total

# Arrays of Square Tiles

NCTM Standards 1, 2, 6, 10

Count the number of square tiles in each part of the array. Write an addition sentence to show the number of tiles in the picture.

1



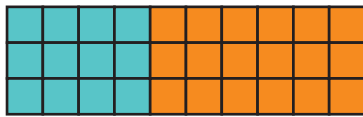
$$\square + \square = \square$$

2



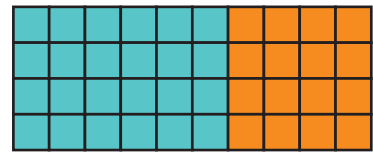
$$\square + \square = \square$$

3



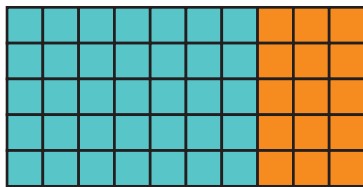
$$\square + \square = \square$$

4



$$\square + \square = \square$$

5



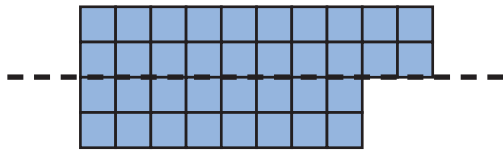
$$\square + \square = \square$$

- 6 Jake put 15 chairs into 3 equal rows. How many chairs were in each row? Draw a picture to show how you solved the problem. Write a number sentence to show your answer.

chairs in each row

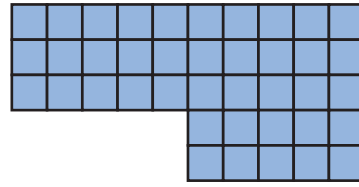
Using vertical or horizontal lines, cut each figure into 2 or 3 rectangular arrays. Write an addition sentence about your picture.

7

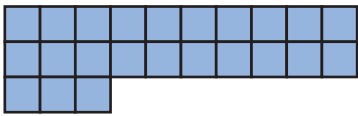


$$20 + 16 = 36$$

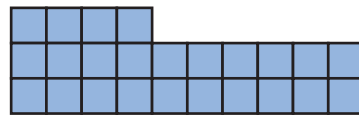
8



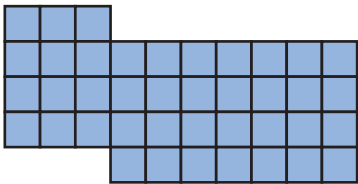

9



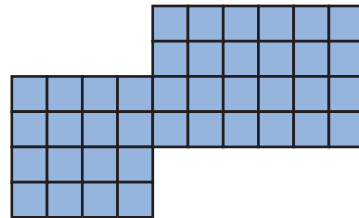

10



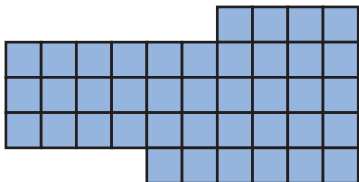

11



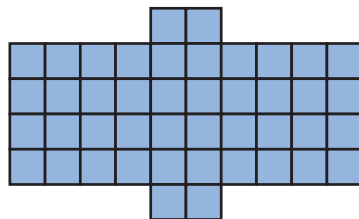

12




**13 Challenge**




**14 Challenge**





# Intersecting Lines

NCTM Standards 1, 2, 6, 7, 8, 9, 10


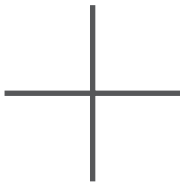

**Use the maps to complete the table.**

**1** Maps with 1 street

<p><b>A</b></p> 	<p><b>B</b></p> 
---------------------------------------------------------------------------------------------------	---------------------------------------------------------------------------------------------------

		A	B
Horizontal —	0		
Vertical	1		
Intersections +	0		

**2** Maps with 2 streets

<p><b>A</b></p> 	<p><b>B</b></p> 	<p><b>C</b></p> 
----------------------------------------------------------------------------------------------------	----------------------------------------------------------------------------------------------------	----------------------------------------------------------------------------------------------------

		A	B	C
Horizontal —				
Vertical				
Intersections +				

**3** Draw maps with 3 streets. Then complete the table.

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>
----------	----------	----------	----------

		A	B	C	D
Horizontal —	0	1	2	3	
Vertical	3	2			
Intersections +			2	0	

4 Draw maps with 4 streets. Then complete the table.

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>

E Draw the missing 4-street map.

		A	B	C	D	E
Horizontal	—	0		2		
Vertical					1	
Intersections	+		3	4	3	

5 Draw maps with 5 streets. Then complete the table.

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>

F Draw the missing 5-street map.

		A	B	C	D	E	F
Horizontal	—	3		5			
Vertical						1	
Intersections	+	6	4	0	0	4	



6 **Challenge** Terrance draws a map with 7 intersections. How many streets does his map have? Use numbers, pictures, or words to explain your answer.

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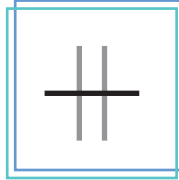
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# Visualizing Intersections

NCTM Standards 1, 6, 10

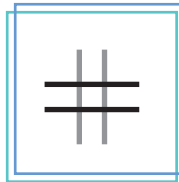
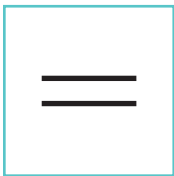
How many horizontal lines? How many vertical lines? How many intersections?

1



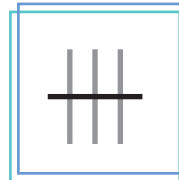
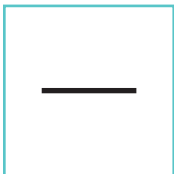
—	1
	2
+	2

2



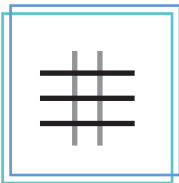
—	
+	

3



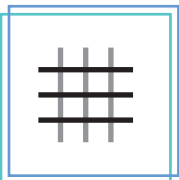
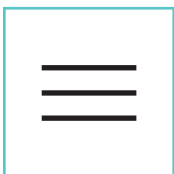
—	
+	

4



—	
+	

5

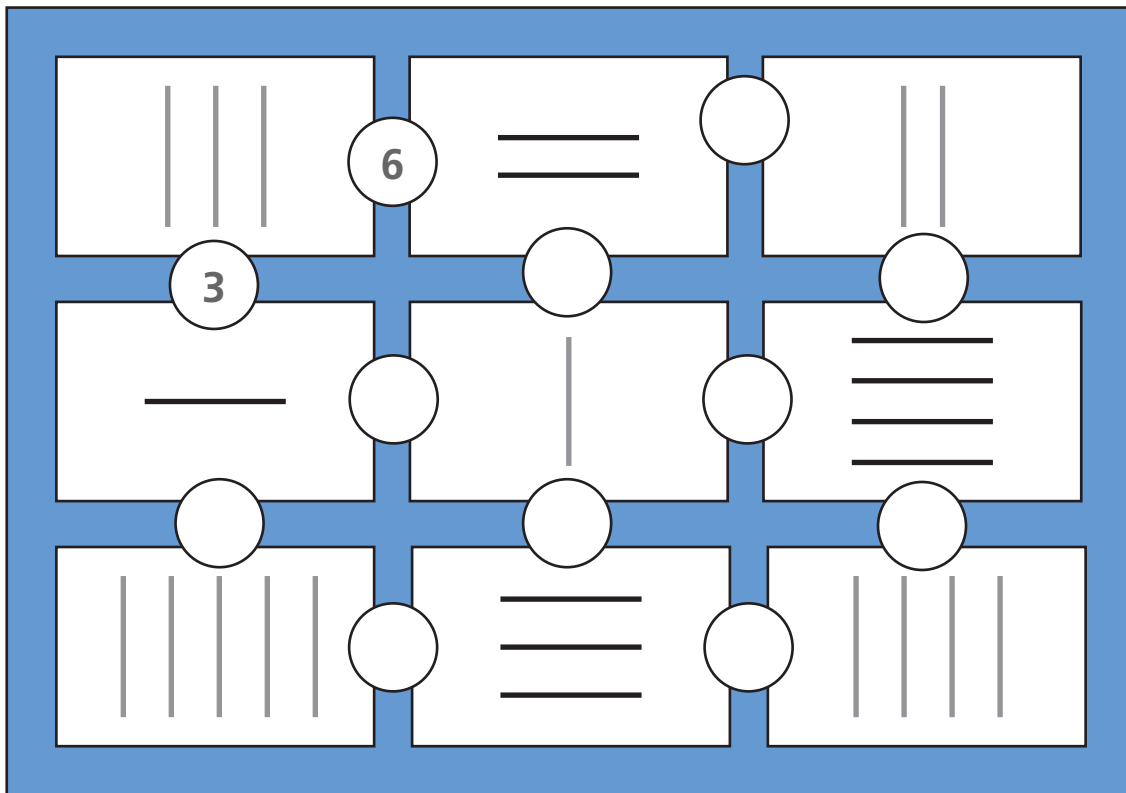


—	
+	

**Solve the problem.**

6 Yuji drew 4 horizontal lines on a transparency. Sandra drew some vertical lines on a transparency. They stacked their transparencies and counted 8 intersections. How many vertical lines did Sandra draw? \_\_\_\_\_

7 Each circle touches two sets of lines. In each circle, write the number of intersections you would see if the two sets of lines were both part of the same map.



8 **Challenge** Complete the table.

—	2		4	3	
		3	4		2
+	6	9		12	8



# Finding the Number of Intersections

NCTM Standards 1, 6, 7, 8, 9, 10

Fill in the missing numbers or the missing maps.

<p><b>1</b></p> <table border="1"> <tr><td>2</td></tr> <tr><td>4</td></tr> <tr><td>6</td></tr> </table>	2	4	6		<table border="1"> <tr><td>4</td></tr> <tr><td>2</td></tr> <tr><td>8</td></tr> </table>	4	2	8	<p><b>KEY</b></p> <ul style="list-style-type: none"> <li> Horizontal</li> <li> Vertical</li> <li> Number of lines</li> <li> Number of intersections</li> </ul>
2									
4									
6									
4									
2									
8									
<p><b>2</b></p> <table border="1"> <tr><td>5</td></tr> <tr><td>1</td></tr> <tr><td>6</td></tr> </table>	5	1	6		<table border="1"> <tr><td>1</td></tr> <tr><td>5</td></tr> <tr><td></td></tr> </table>	1	5		
5									
1									
6									
1									
5									
<p><b>3</b></p> <table border="1"> <tr><td>1</td></tr> <tr><td>3</td></tr> <tr><td>4</td></tr> </table>	1	3	4		<table border="1"> <tr><td>3</td></tr> <tr><td>1</td></tr> <tr><td></td></tr> </table>	3	1		
1									
3									
4									
3									
1									
<p><b>4</b></p> <table border="1"> <tr><td>4</td></tr> <tr><td>3</td></tr> <tr><td></td></tr> </table>	4	3			<table border="1"> <tr><td></td></tr> <tr><td></td></tr> <tr><td></td></tr> </table>				
4									
3									
<p><b>5</b></p> <table border="1"> <tr><td>1</td></tr> <tr><td>1</td></tr> <tr><td></td></tr> </table>	1	1			<table border="1"> <tr><td></td></tr> <tr><td></td></tr> <tr><td></td></tr> </table>				
1									
1									



**6** A tiny town has 6 streets and 8 intersections. Draw a map of the town. Explain how you found your answer.

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Use the information in the table and in the pictures to complete the maps and fill in the table.

7



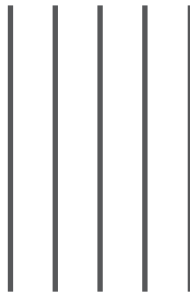
8



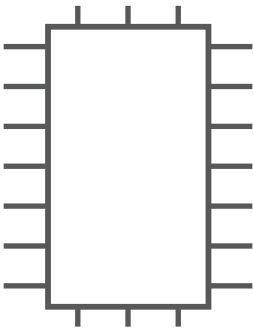
9



10

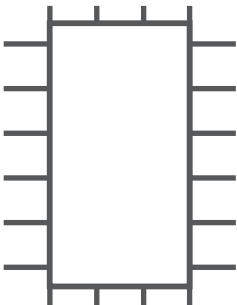


11



12

13



14 **Challenge**

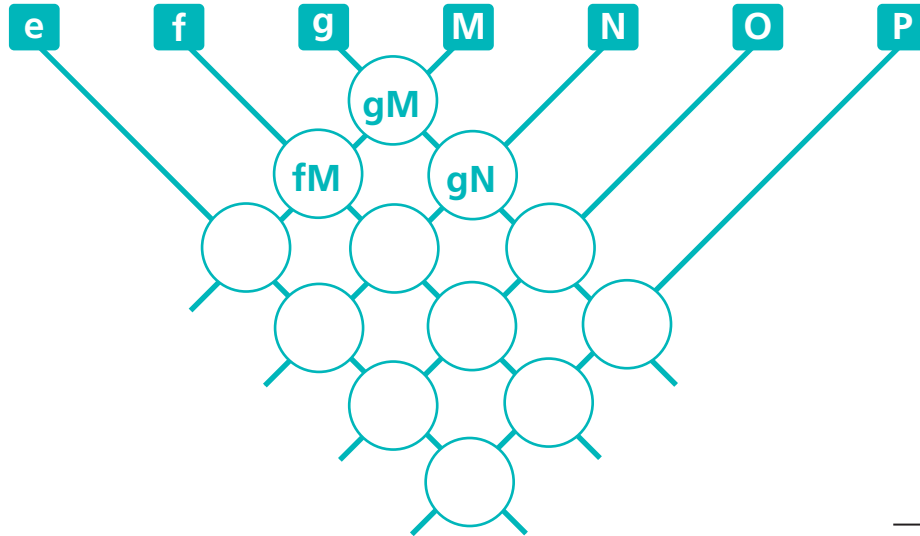
	-		+
7	3		
8		5	
9		4	
10	6		
11	7	3	
12	3		18
13	6	4	
14			5

# Pairing Objects

NCTM Standards 1, 2, 6, 8, 9, 10

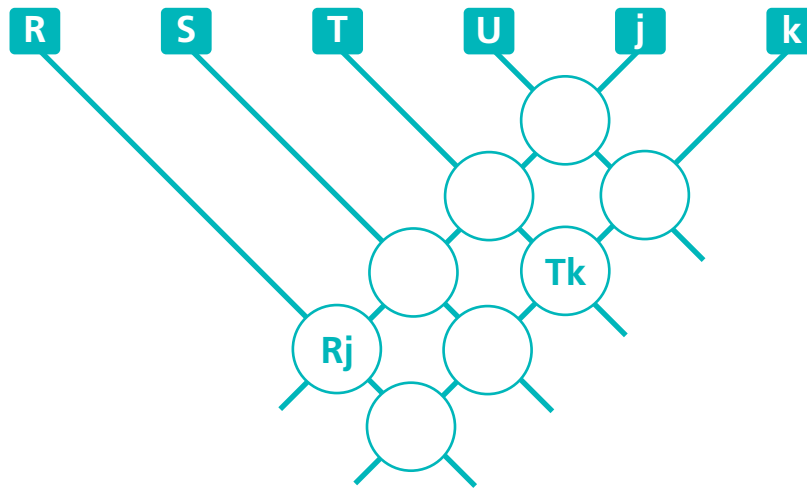
List all the pairs. Write the number of pairs.

1



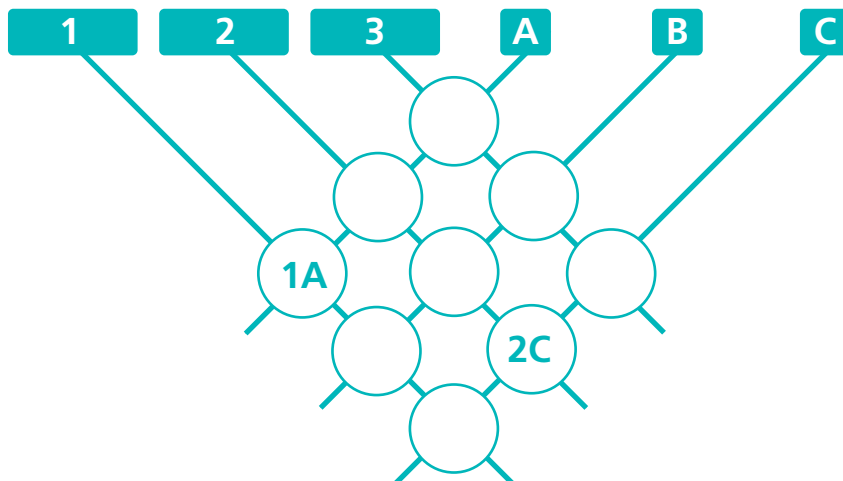
\_\_\_\_\_ pairs

2



\_\_\_\_\_ pairs

3



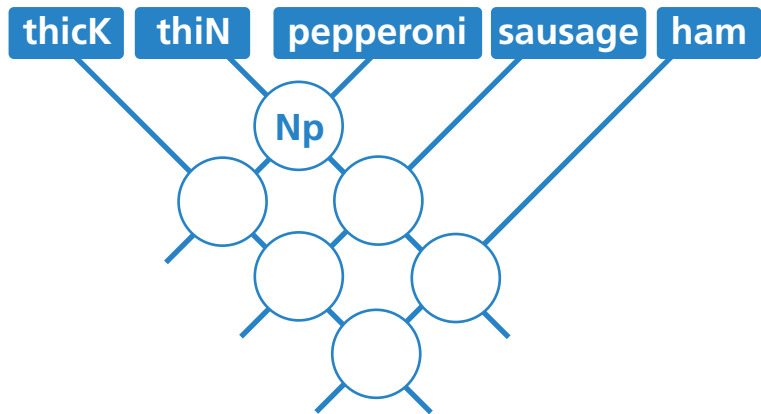
\_\_\_\_\_ pairs



Vegetables	Meat	Crust
green peppers	pepperoni	thick
onions	sausage	thin
black olives	ham	
mushrooms		

4 How many different pizzas can you make if you choose one kind of crust and one kind of meat?

\_\_\_\_\_ pizzas



5 Customers can order a thin crust pizza with one meat and one vegetable. How many choices do the customers have?

\_\_\_\_\_ choices



6 **Challenge** How many thin crust pizzas can you make with three kinds of vegetables and no meat? Explain how you know.

\_\_\_\_\_

\_\_\_\_\_

# Listing Combinations

NCTM Standards 1, 2, 6, 9, 10

List all of the two-digit numbers by using a tens digit from the shaded box and a ones digit from the white box.

1

4, 7	0
------	---

4	0	7	0	X	X
---	---	---	---	---	---

2	two-digit numbers
---	-------------------

	×	1	=	
choices for the tens digit		choices for the ones digit		number of two-digit numbers

2

4, 5	0, 1, 2, 3
------	------------

	two-digit numbers
--	-------------------

	×		=	
choices for the tens digit		choices for the ones digit		number of two-digit numbers

3

1, 2, 3	1, 2, 3
---------	---------

	two-digit numbers
--	-------------------

	×		=	
choices for the tens digit		choices for the ones digit		number of two-digit numbers

## One Sandwich **with** One Topping

Hamburger  
Hot Dog  
Fish

Onions  
Ketchup  
Mustard  
Pickles

- 4 Predict the number of combinations of one kind of sandwich with one kind of topping.

$$\square \times \square = \square$$

sandwiches      toppings      combinations

- 5 List all the combinations for one kind of sandwich with one topping.

<input type="text"/>	with	<input type="text"/>	<input type="text"/>	with	<input type="text"/>
<input type="text"/>	with	<input type="text"/>	<input type="text"/>	with	<input type="text"/>
<input type="text"/>	with	<input type="text"/>	<input type="text"/>	with	<input type="text"/>
<b>hamburger</b>	with	<b>pickles</b>	<input type="text"/>	with	<input type="text"/>
<input type="text"/>	with	<input type="text"/>	<input type="text"/>	with	<input type="text"/>
<input type="text"/>	with	<input type="text"/>	<input type="text"/>	with	<input type="text"/>

- 6 **Challenge** Donna will not eat pickles or onions. Write a multiplication sentence to find the number of combinations of one kind of sandwich with one topping that Donna will eat.

- 7 **Challenge** Dino will not eat hot dogs or hamburgers. Write a multiplication sentence to find the number of combinations of one kind of sandwich with one topping that Dino will eat.

## Using Multiplication

NCTM Standards 1, 2, 6, 8, 9, 10

Write a multiplication sentence to describe each array.

1



$$\square \times \square = \square$$

rows columns dots

2



$$\square \times \square = \square$$

rows columns dots

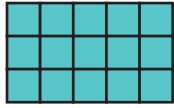
3



$$\square \times \square = \square$$

rows columns dots

4



$$\square \times \square = \square$$

rows columns tiles

5



$$\square \times \square = \square$$

rows columns tiles

6



$$\square \times \square = \square$$

rows columns tiles

7



$$\square \times \square = \square$$

rows columns dots

8



$$\square \times \square = \square$$

rows columns dots

9



$$\square \times \square = \square$$

rows columns dots

10



$$\square \times \square = \square$$

rows columns dots

11



$$\square \times \square = \square$$

rows columns dots

12



$$\square \times \square = \square$$

rows columns dots

13



$$\square \times \square = \square$$

rows columns tiles

14



$$\square \times \square = \square$$

rows columns tiles

15

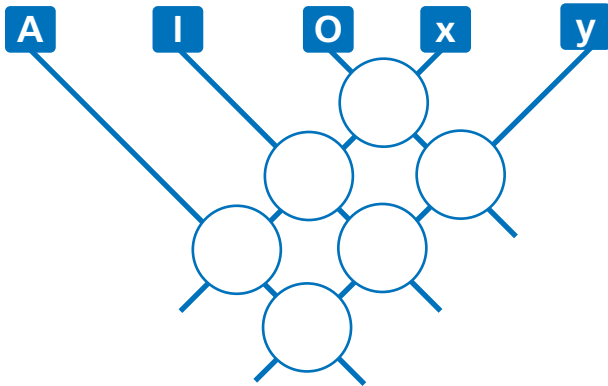


$$\square \times \square = \square$$

rows columns tiles

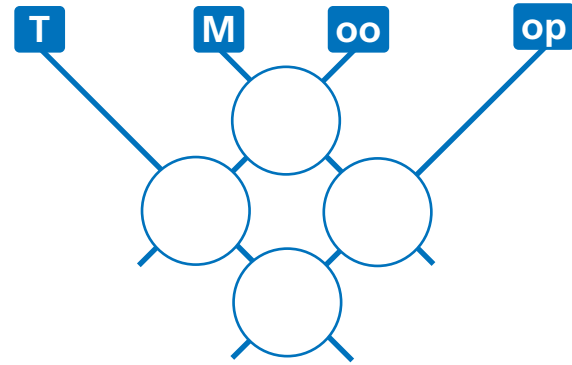
Complete the diagram. Write a multiplication sentence to match.

16



$$\square \times \square = \square$$

17



$$\square \times \square = \square$$



18 Min has three kinds of ice cream and two kinds of toppings. How many different one flavor–one topping sundaes can she make? Use words, pictures, or numbers to explain your answer.

sprinkles hot fudge vanilla chocolate strawberry



\_\_\_\_\_ sundaes



19 **Challenge** If Min gets two new toppings and one new flavor of ice cream, how many one flavor–one topping sundaes can she make with all of the flavors and toppings she has now? Use words, pictures, or numbers to explain your answer.

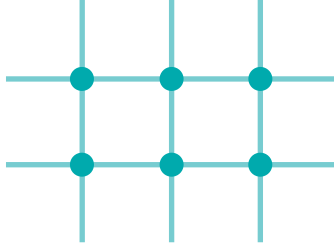


# Writing Number Sentences for Intersecting Lines

NCTM Standards 1, 2, 6, 7, 8, 10

Fill in the blanks.

1



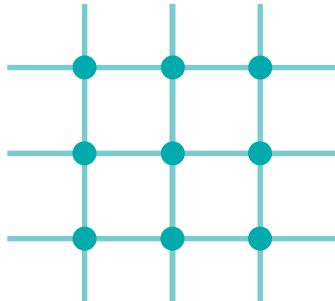
Number of lines:

$$\boxed{2} + \boxed{3} = \boxed{\phantom{00}}$$

Number of intersections:

$$\boxed{2} \times \boxed{3} = \boxed{\phantom{00}}$$

2



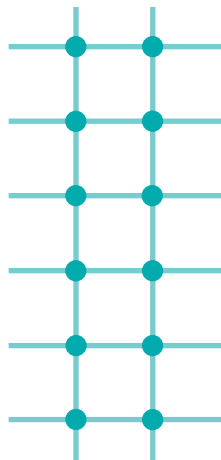
Number of lines:

$$\boxed{\phantom{00}} + \boxed{\phantom{00}} = \boxed{\phantom{00}}$$

Number of intersections:

$$\boxed{\phantom{00}} \times \boxed{\phantom{00}} = \boxed{\phantom{00}}$$

3



Number of lines:

$$\boxed{\phantom{00}} + \boxed{\phantom{00}} = \boxed{\phantom{00}}$$

Number of intersections:

$$\boxed{\phantom{00}} \times \boxed{\phantom{00}} = \boxed{\phantom{00}}$$

Complete the maps and the number sentences.

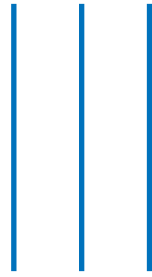
4



$$\boxed{6} + \boxed{\phantom{00}} = \boxed{9}$$

$$\boxed{6} \times \boxed{\phantom{00}} = \boxed{\phantom{00}}$$

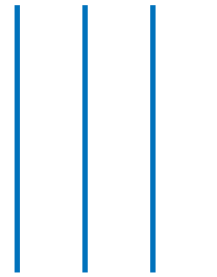
5



$$\boxed{\phantom{00}} + \boxed{3} = \boxed{\phantom{00}}$$

$$\boxed{\phantom{00}} \times \boxed{3} = \boxed{15}$$

6



$$\boxed{\phantom{00}} + \boxed{4} = \boxed{\phantom{00}}$$

$$\boxed{\phantom{00}} \times \boxed{4} = \boxed{16}$$



7 Phillip drew a map with 8 intersections. When he added the number of streets, he got an even number. Describe Phillip's map.

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**8 Challenge** Find all the ways to make 24 intersections.

vertical horizontal

$$\boxed{\phantom{00}} \times \boxed{\phantom{00}} = \boxed{24}$$

$$\boxed{\phantom{00}} \times \boxed{\phantom{00}} = \boxed{24}$$

$$\boxed{\phantom{00}} \times \boxed{\phantom{00}} = \boxed{24}$$

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$$\boxed{\phantom{00}} \times \boxed{\phantom{00}} \quad \boxed{24}$$

$$\boxed{\phantom{00}} \times \boxed{\phantom{00}} \quad \boxed{24}$$

# Breaking Products into Factors

NCTM Standards 1, 2, 6, 7, 9, 10

**A map has 14 intersections and 2 vertical streets.**

1 Draw the map.

2 How many horizontal streets are there?

horizontal streets

3 Solve.

$$2 \times \square = 14$$

$$14 \div 2 = \square$$

**16 dots are arranged in a rectangular array.  
The array has 4 rows.**

4 Draw the array.

5 How many columns are there?

columns

6 Solve.

$$4 \times \square = 16$$

$$16 \div 4 = \square$$

**6 boys are sharing 18 pretzels.**

7 Draw a picture to show how many pretzels each boy would get.

Each boy gets  pretzels.

8 Solve.

$$6 \times \square = 18$$

$$18 \div 6 = \square$$

For each number of intersections, draw a map and complete the multiplication sentence.

9

15 intersections

$$\square \times \square = 15$$

10

9 intersections

$$\square \times \square = 9$$

11

10 intersections

$$\square \times \square = 10$$

12

21 intersections

$$\square \times \square = 21$$

**13 Challenge** Draw all the maps with 12 intersections.

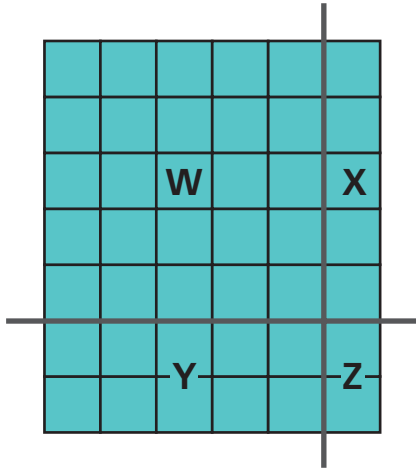
List all the factors of 12: \_\_\_\_\_

# Separating Arrays

NCTM Standards 1, 2, 7, 9, 10

Write a multiplication sentence for each part of the big array. Find the number of the tiles in the parts to finish the multiplication sentence for the big array.

1



W: 5 5

X: 5 1

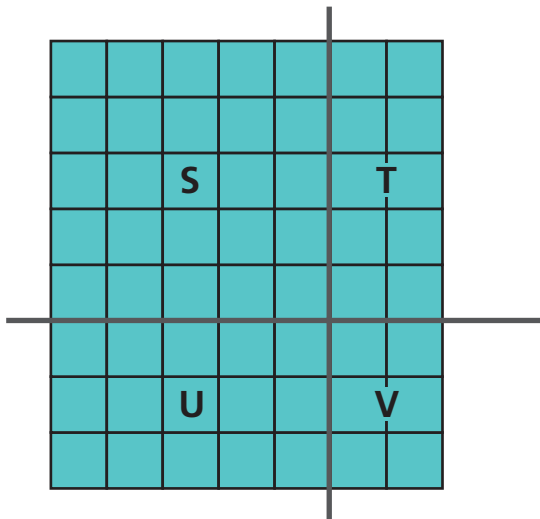
Y: 2 5

Z: 2 1

W X Y Z

7 6

2



S:

T:

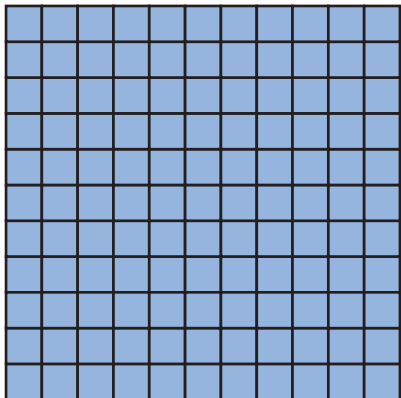
U:

V:

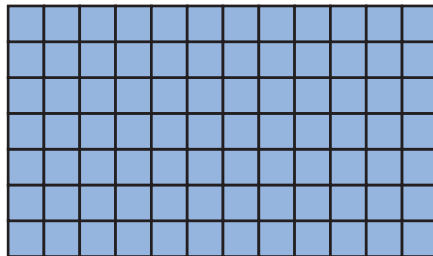
S T U V

Separate each array into two, three, or four parts. Label each part with its number of tiles. Find the sum of the tiles in the parts to finish the multiplication sentence for the big array.

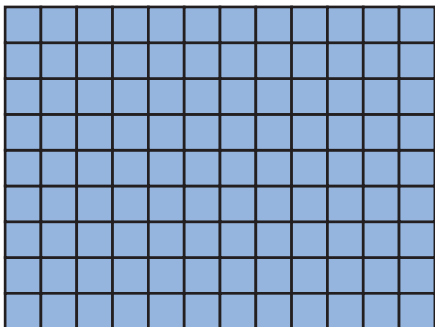
3



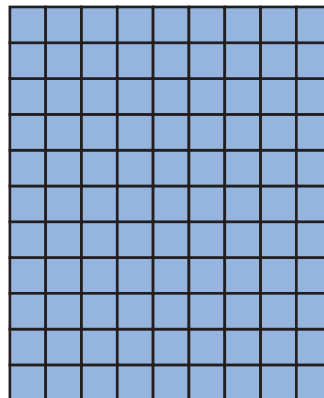
4



5



6

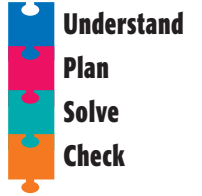


**7 Challenge** Fill in the missing numbers in this number sentence. (Think about separating a big array into parts.)

$$(10 \times 10) + (4 \times \square) + (\square \times 10) + (3 \times \square) = 14 \times 13$$

**Problem Solving Strategy****Draw a Picture**

NCTM Standards 1, 6, 7, 8, 9, 10



**Solve each problem. Use the large white space to draw a picture if you want.**

- 1 The Writing Store has pens, pencils, crayons, chalk, and markers. Each writing tool comes in blue, green, and red. How many different items do they sell?

\_\_\_\_\_

- 2 Max has 27 pennies. He makes 3 equal stacks. How many pennies are in each stack?

\_\_\_\_\_

- 3 Leticia begins her art project by drawing 7 lines on her paper. She draws some horizontal lines and some vertical lines. How many intersections can she make with the 7 lines?

\_\_\_\_\_

- 4 Connor needs 30 batteries for his science project. There are 4 batteries in 1 package. If he buys 7 packages, will he have enough batteries? Explain.

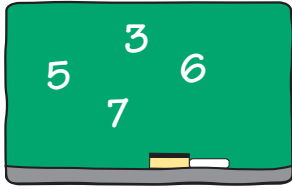
\_\_\_\_\_

\_\_\_\_\_

# Problem Solving Test Prep

Choose the correct answer.

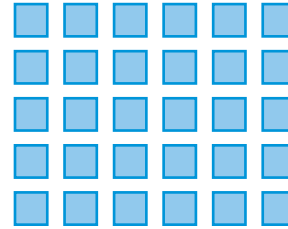
- 1 Miss Reef wrote these four digits on the board:



What is the largest possible four-digit number you can write with these digits?

- A. 5,367      C. 7,563  
B. 6,357      D. 7,653

- 2 Which number completes the number sentences?



$$5 \times \blacksquare = 30, 30 \div 5 = \blacksquare$$

- A. 6      C. 1  
B. 5      D. 0

## Show What You Know

Solve each problem. Explain your answer.

- 3 Mr. Gomez will give his son 1 type of fruit and 1 type of cereal for breakfast. He can choose from 3 types of fruit and 2 types of cereal. How many different combinations of 1 fruit and 1 cereal are possible? Explain how you know.

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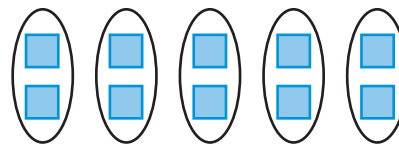
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- 4 What multiplication sentence can you write for  $2 + 2 + 2 + 2 + 2 = 10$ ? Explain how you know.



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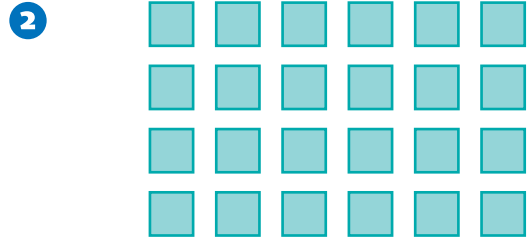
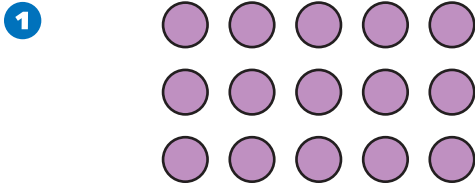
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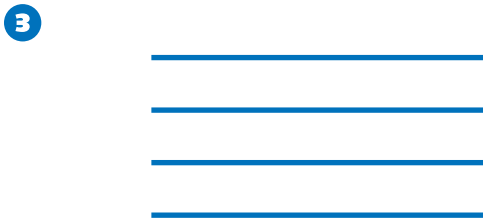
## Review/Assessment

NCTM Standards 1, 2, 6, 7, 9, 10

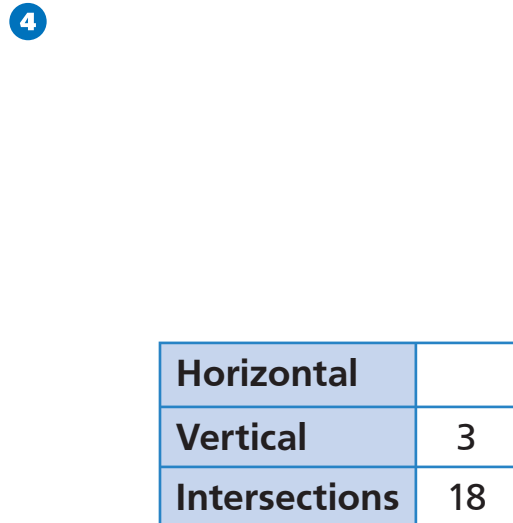
Write the number of dots or tiles in each picture. Lessons 1, 2, and 11



Complete the map and the table. Lessons 3, 4, and 5



Horizontal	4
Vertical	5
Intersections	



Horizontal	
Vertical	3
Intersections	18

5 There are 4 hikers and 2 bicyclists. Every hiker shakes hands with every bicyclist. How many handshakes are there? Lessons 6 and 7 \_\_\_\_\_ handshakes

- 6 Find all the two-digit numbers with a tens digit from the shaded box and a ones digit from the white box. *Lessons 6 and 7*

3, 6	0, 2, 4
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\_\_\_\_\_ two-digit numbers

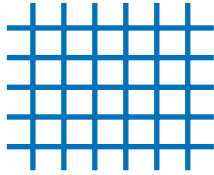
**Write a multiplication sentence for Problems 7 and 8.** *Lessons 8 and 9*

7

● ● ● ● ● ● ● ● ●

□ □ □

8



□ □ □

- 9 9 dots are arranged in a rectangular array. The array has 3 rows. Draw the array. *Lesson 10*

Solve: 3 □ 9

- 10 A map has 14 intersections and 2 horizontal streets. Draw the map. *Lesson 10*

Solve: 2 □ 14

**Solve the problem.** *Lesson 12*

- 11 Three girls are sharing 27 grapes. They each will get the same amount. How many grapes will each girl get?

\_\_\_\_\_ grapes