$\qquad$

## Introducing Arrays

## Write the fact family for each diagram.

The first one is done for you.

(9) How does the number of sentences in a fact family with 2 identical factors compare to the number of sentences in a fact family with 2 different factors?
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Separating Arrays

Find the total number of tiles in each array.
(1) $\frac{\square}{\square}$
$(1 \times 3)+(3 \times 3)-3+9=\square$
2


$$
(4 \times 2)+(4 \times 1)=8+4=\square
$$

(4)

$(5 \times 2)+(5 \times 4)=\square+\square=\square$

$(3 \times 5)+(5 \times 5)=\square+\square=\square$

$(4 \times 5)+(3 \times 5)=\square+\square=\square$
©

$(8 \times 4)+(8 \times 1)=\square+\square=\square$
8

$(7 \times 2)+(7 \times 3)=\square+\square=\square$

## Adding Array Sections

Write the multiplication sentence shown by each part of the array. Find the sum of all the parts to find the total number of squares in the array.
(1)

2


3

$\qquad$
$\qquad$
$\qquad$
(4)

$\qquad$

## Exploring a Multiplication Shortcut

Find the number of squares in each array.
1
13


$$
5 \times 13=\square
$$

2


$$
8 \times 16=\square
$$

$\qquad$

## Using a Multiplication Shortcut

For Problem 1, use the figure.
(1) Number of rows in the figure $\qquad$


Number of rows + Number of columns $\qquad$
Complete the drawing.
How many small squares in all? $\qquad$
Two numbers that have a sum of 10 and a product
of 24 are $\qquad$ and $\qquad$ .

For Problems 2-8, find two numbers that have
(2) a product of 30 and a difference of 7 $\qquad$ and $\qquad$
(3) a product of 45 and a difference of 4 $\qquad$ and $\qquad$
(4) a product of 60 and a difference of 4 $\qquad$ and $\qquad$
(5) a product of 36 and a sum of 12 $\qquad$ and $\qquad$
(6) a product of 25 and a difference of 0 $\qquad$ and $\qquad$
(7) a product of 4 and a sum of 4 $\qquad$ and $\qquad$
(8) a product of 18 and a sum of 11 $\qquad$ and $\qquad$
(2) Create a product-and-sum or product-and-difference puzzle. Exchange with a partner and solve.

## Connecting Multiplication and Division

(1) Find the three numbers that are common to both lists.
$\qquad$
$\qquad$ , and $\qquad$
A: 121518212427303336394245485154576063666972
B: 212835424956637077849198

I multiplied my secret number by several other numbers and got 21,42 , and 63 . My secret number is greater than 1 and less than 10 . There is more than one possibility. What could my secret number be?

My secret number could be $\qquad$ or $\qquad$ .
(2) Find the number that is common to all lists. $\qquad$
A: 8101214161820222426
283032343638404244

B: 1520253035404550556065707580859095100
C: 1624324048566472808896
I multiplied my secret number by another number and got 40. My secret number is greater than 1 and less than 10 . There is more than one possibility. What could my number be?

My secret number could be $\qquad$ or $\qquad$ or $\qquad$
(3) I multiplied several numbers by my secret number and got $24,36,54$. If my secret number is greater than 1, what is my secret number? There is more than one possibility.
(4) I multiplied several numbers by my secret number and got 36,48 , and 60 . How many possibilities can you find for my secret number? What are they?

## Arrays with Leftovers

I divided some numbers by a secret number. Each table shows a different pattern. Find the secret number in each case.

| Number divided | 9 | 17 | 23 | 35 | 41 | 45 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Remainder | 1 | 1 | 1 | 1 | 1 | 1 |

My secret number is $\qquad$ .

2

| Number divided | 18 | 22 | 34 | 40 | 59 | 67 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Remainder | 8 | 2 | 4 | 0 | 9 | 7 |

My secret number is $\qquad$
3

| Number divided | 12 | 14 | 16 | 21 | 35 | 39 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Remainder | 0 | 2 | 0 | 1 | 3 | 3 |

My secret number is $\qquad$ .

| Number divided | 15 | 20 | 25 | 30 | 35 | 40 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Remainder | 3 | 2 | 1 | 0 | 5 | 4 |

My secret number is $\qquad$ .

| Number divided | 19 | 22 | 25 | 28 | 31 | 34 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Remainder | 1 | 1 | 1 | 1 | 1 | 1 |

My secret number is $\qquad$ .

| Number divided | 23 | 28 | 35 | 41 | 46 | 51 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Remainder | 3 | 3 | 0 | 1 | 1 | 1 |

My secret number is $\qquad$ .

## Working with Remainders

Sammy brought fewer than 21 cookies to share with friends. He put some on the table. The rest are in the bag.
(1) Sammy shared his cookies equally with
 4 friends. Some cookies were left over.

| Number of <br> cookies | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Left over | 3 | 4 | 0 | 1 | 2 | 3 | 4 | 0 |

When you divide by 5 , what remainders are possible? $\qquad$
(2) Sammy shared his cookies equally with 6 friends.

Some cookies were left over.

| Number of <br> cookies | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Left over | 6 | 0 | 1 | 2 | 3 | 4 | 5 | 6 |

When you divide by 7, what remainders are possible? $\qquad$
(3) What remainders are possible when you divide by the following numbers?
A. by 2
C. by 4
B. by 3 $\qquad$ D. by 6

Make up a rule that tells what remainders are possible for any divisor.

